Optimization in optical systems revisited

Beyond genetic algorithms

Denis Gagnon, Joey Dumont and Louis J. Dubé

Département de physique, de génie physique, et d'optique, Université Laval, Québec, Canada

Optimization in physics

Optimization problems are ubiquitous in physics. Notable instances include

- Design of integrated optical devices
- Design of injectors and magnets in accelerator design
- Topological solitons in nonlinear classical field theories
- ➡ Ising models in condensed matter physics

Most real-life optimization problems cannot be solved analytically and are NP-hard. The most common approach is to use metaheuristics, algorithms based on empirical rules for exploring large solution spaces

Two key concepts for metaheuristics

1. Diversification: Global exploration of the solution space in order to identify regions containing "fit" solutions

2. Intensification: More thorough investigation of "promising" solution regions [1].

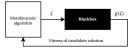
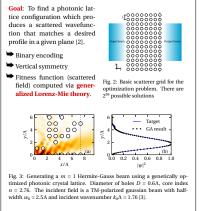


Fig. 1: Blackbox scenario for fitness function evaluation [1]

Laser beam shaping problem



Genetic algorithm

Developed by J. Holland in the 1970's. Commonly used in photonics research, for instance integrated waveguide design [2].

- Stochastic, population-based, nature-inspired algorithm
- Memoryless method. The escape from local minima relies on random mutations
- Best suited for diversification. This stems from the population based nature of the algorithm
- 3 adjustable parameters to specify: Population size, mutation and crossover rates

Application to single-objective optimization

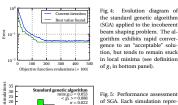
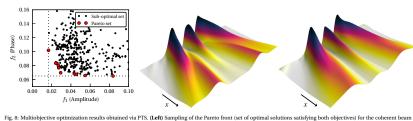


Fig. 5: Performance assessment of SGA. Each simulation represents 5000 generations, with an average of 60 objective function evaluations per generation. 6 0.08 0.10 0.12 0.14 0.1 Final value of g





shaping problem. The dotted lines indicate the best possible value for each of the two objectives. This sampling is achieved using an aggregate cost function. (Center) Optimized Hermite-Gauss beam profile at device output, with the best possible reproduction of the amplitude profile. (Right) Best possible trade-off between the two objectives. Since the phase is controlled, the Hermite-Gauss profile shape is preserved over a greater propagation distance. In other words, controlling both the amplitude and the phase allows for a greater field depth. This can be seen in the smaller number of ridges in the profile [4]

Aggregation method		Amplitude objective function	Phase objective function
$\min_{\xi \in \Xi} \sum_{i=1}^{p} \alpha_i f_i(\xi),$	$f_i = \frac{g_i}{g_i^{\max}}$	$g_1(\xi) = \frac{\int \left u(x_0, y) ^2 - \bar{u}(x_0, y) ^2 \right dy}{\int \bar{u}(x_0, y) ^2 dy}$	$g_2(\xi) = \frac{\int \left \text{Im}[u(x_0, y)e^{-i\phi(x_0, 0)}] \right ^2 dy}{\int \bar{u}(x_0, y) ^2 dy}$

Parallel tabu search

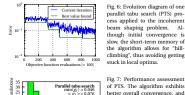
First proposed by F. Glover in the 1980's. More commonly used in scheduling and networking problems

Deterministic, local, non-nature inspired algorithm [1]

- ➡ Uses a **short-term memory** to escape from local minima
- Best suited for intensification of search. Parallel implementation allows to combine exploration and intensification. Initialization of solutions is the only random process

Only 1 adjustable parameter: Number of entries in the Tabu

Application to single-objective optimization



Final value of g

slow, the short-term memory of the algorithm allows for "hillclimbing", thus avoiding getting stuck in local optima. Fig. 7: Performance assessment of PTS. The algorithm exhibits

better overall convergence, and finds some solutions inaccessi ble to the SGA Each simulation represents 5000 iterations, with at most 56 objective func-

tion evaluations per iteration.

UNIVERSITÉ



Outlooks

Engineering of non-diffracting beams

Non-diffracting beams can be used in many applications, like atom guiding and microscopy. Various generation methods have been proposed.

- Axicon-shaped photonic crystals [H. Kurt, J. Opt. Soc. Am. B 26, 981 (2009)]
- Phase plates optimized via GA [P. A. Sanchez-Serrano et al., Opt. Lett. 37, 5040 (2012)]
- Huygens' surfaces, composed of 2D arrays of polarizable particles [C. Pfeiffer and A. Grbic, PRL 110, 197401+ (2013)]

Optimization of random laser action

Recent studies have shown that optimizing the pump shape allows control of laser thresholds and emission directionality This optimization process implies the computation of a special kind of eigenstate, the constant-flux state [5].



Fig. 9: Constant-flux state of an asymmetric photonic molecule composed of 4 dielectric atoms. Emission profile computed via gen eralized Lorenz-Mie the ory. Constant-flux states are more physically meaningful than the usual quasi bound states

Summary

- 1. Since parallel tabu search combines search diversification and intensification, it outperforms the SGA in the case of our model problem of beam shaping.
- 2. The performance gain associated with PTS allows for multiobjective optimization in photonics design
- 3. Optimization of random lasers and engineering non diffract ing beams are potential applications of our algorithms in optics and photonics.

References

- [1] E.-G. Talbi, Metaheuristics : From design to implementation (Wiley, 2009)
- [2] A. Vukovic, P. Sewell, and T. M. Benson, J. Opt. Soc. Am. A 27, 2156 (2010) [3] D. Gagnon, J. Dumont, L. J. Dubé, J. Ont. Soc. Am, A 29, 2673 (2012)
- [4] D. Gagnon, J. Dumont, L. J. Dubé, To appear in Opt. Lett. (2013)
- 5] T. Hisch, M. Liertzer, D. Pogany, F. Mintert, and S. Rotter (2013), arxiv:1303.529

The authors thank Prof. Alain Hertz for an introduction to the world of metaheuristics. JD is grateful to the CERC in Enabling Photonic Innovations for Information and Con cation for a research fellowship. Computations were made on the supercomputer Colosse from Université Laval, managed by Calcul Québec and Compute Canada.



denis.gagnon.6@ulaval.ca http://www.dynamica.phy.ulaval.ca/ ljd@phy.ulaval.ca